

Here's a brief summary of Scheme for the purposes of project 1.

Scheme data

There are two main data types in Scheme: symbols (which include numbers), and lists. A list is displayed with parentheses enclosing the list elements, for example:

```
(a b 3)
```

A list may be empty; the empty list, displayed as `()`, is named NIL. List elements may also be lists themselves, for example:

```
((a b) (x ( ) (3 4 5)))
```

Evaluation of Scheme expressions

A Scheme expression is either a symbol or a list that may be provided as input to the interpreter. The interpreter executes a loop with the following steps:

1. read the next symbol or list from the user;
2. evaluate it;
3. print the result.

Evaluation is conceptually a big switch:

1. A numeral's value is the corresponding numeric value.
2. A symbol's value is what it gets initialized to via the `define` function (see below). If the symbol has not been provided as an argument to `define`, the error message "undefined variable" results.
3. A quoted expression's value is the expression itself, taken literally. For example, the value of `'(a b)` is the list `(a b)`. Within a quoted expression, the quote translates to a call to the function `quote`; thus `'(a b '(x y))` would evaluate to the list `(a b (quote (x y)))`.
4. A parenthesized expression is evaluated differently, depending on whether or not it is a *special form*. In a special form, the word following the left parenthesis is either `quote` or `define`.

The `quote` function takes a single argument, the "quoted" expression; the value of a call to `quote` is the quoted expression. Thus the value of the expression `(quote (a b))` is the list `(a b)`.

The `define` function declares and initializes a variable. The variable declared/initialized is the first argument of `define`; the value it's initialized to is the result of evaluating the second argument. If a variable is used before it appears in a `define` expression, an "undefined variable" error message results. A second `define` for a variable merely replaces the value associated with that variable.

5. Otherwise, the first thing after the left parenthesis must name one of the functions `+`, `cons`, `car`, or `cdr`, and the remaining things that precede the right parenthesis are arguments. The value is computed by recursively evaluating the arguments, then applying the function to them.

Builtin functions

The `cons` function (short for “construct”) takes two arguments, a Scheme expression and a Scheme list. It returns a *pair* whose “`car`” (first element) is the value of the first argument and whose “`cdr`” (second element) is the value of the second argument. A pair whose second element is a list is itself a list. Thus lists may be defined recursively:

A list is either empty—printed as `()`—or the result of evaluating a call to `cons` with a list as the second argument.

A pair that’s not a list is displayed with a dot between the elements of the rightmost `cons`.

Here are some examples.

expression	displayed value
<code>(cons 1 (cons 2 3))</code>	<code>(1 2 . 3)</code>
<code>(cons 1 '(2 3))</code>	<code>(1 2 3)</code>
<code>(cons 'a '(b c))</code>	<code>(a b c)</code>
<code>(cons '(b c) '(a x))</code>	<code>((b c) a x)</code>

Note that leaving out the quotes in `(cons 'a '(b c))`, thus trying to evaluate the expression `(cons a (b c))`, would result in trying to evaluate the symbol `a`, which is fine if `a` has been define’d, and the expression `(b c)`, which is a call to the function named `b` and is thus not allowed in this project.

The `car` and `cdr` functions each take a pair—the result of some `cons` operation—as argument, and return the first or second element of the pair, respectively. Examples:

expression	displayed value
<code>(car (cons 'a '(a b c)))</code>	<code>a</code>
<code>(car '((x y) z))</code>	<code>(x y)</code>
<code>(cdr (cons 'a '(a b c)))</code>	<code>(a b c)</code>
<code>(cdr '((x y) z))</code>	<code>(z)</code>

The `+` function takes two numeric values as arguments and returns their sum.