- 1. List all the procedures in the metacircular evaluator that call mc-eval.
- 2. List all the procedures in the metacircular evaluator that call mc-apply.
- 3. Abelson and Sussman, exercise 4.1
- 4. In this exercise, we will begin to write a postfix version of the metacircular evaluator. For now, do not worry about special forms; we will only provide postfix support for procedure calls, self-evaluating expressions, etc.
- a. Make a new copy of mceval.scm and call it postfix-mceval.scm (we don't want these changes to conflict with future exercises). Make all changes for this exercise in postfix-mceval.scm.
- b. Our postfix expressions will look the same as our prefix expressions, except that the operator will go on the right. Examples:

```
(2 3 +)
(((3 1 +) 8 *) 9 -)
('(one no trump) car)
```

To make this somewhat efficient (by only looking at each subexpression once), we will maintain a stack in mc-eval. The purpose of this stack is to keep track of evaluated subexpressions until we get to the operator.

Example: We want to evaluate (2 (3 4 +) +)

```
\rightarrow mc-eval called with exp = (2 (3 4 +) +) stack = () ;; not at operator yet
   -> mc-eval called with exp = 2 stack = ()
                                                         ;; .. so evaluate first arg
\rightarrow mc-eval called with exp = ((3 4 +) +) stack = (2)
                                                        ;; not at operator yet -> evaluate 2nd arg
   -> mc-eval called with exp = (3 4 +) stack = ()
                                                         ;; .. second arg is a nested exp
      -> mc-eval called with exp = 3 stack = ()
                                                         ;; .... evaluate 1st arg of nested exp
   \rightarrow mc-eval called with exp = (4 +) stack = (3)
                                                        ;; .. not at operator yet
     -> mc-eval called with exp = 4 stack = ()
                                                        ;; .... evaluate 2nd arg of nested exp
   -> mc-eval called with exp = (+) stack = (3 4)
                                                        ;; .. found the operator
      -> mc-eval called with exp = + stack = ()
                                                        ;; .... so evaluate op and perform operation
-> mc-eval called with exp = (+) stack = (2 7)
                                                        ;; found the operator
                                                         ;; .. so evaluate op and perform operation
```

As you can see, everytime we start evaluating a new expression, we start with an empty stack. At the top of mceval.scm, give a definition of the-empty-stack, which will be used to represent such an empty stack.

- c. Modify the code for mc-eval so that it now takes in an additional argument: the stack
- d. Modify the application? clause of mc-eval so that it deals with postfix expressions and exhibits the behavior in the example in step b. Do not worry about data abstraction.
- e. Modify the code so that all calls to mc-eval have an appropriate stack.
- f. Try it out!
- g. Given the current modifications, what types of expressions will not work in postfix notation. What additional modifications are necessary?